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Property Driven Models: Experimental Validations and Simplifications

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- 1. Models and Formal Logic
- 2. Gene Networks and Temporal Logic
- 3. Extracting Experiments from Models
- 4. Model Simplifications
- 5. Circadian Circle, Seasons and Jet-lag

Mathematical models: what for ?

- Models as "Data Base" to store biological knowledge
- Models as design tools
- Models as logical analysis of causality chains
- Models as guidelines for the choice of experiments

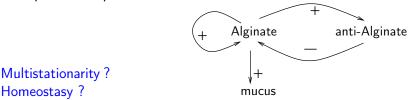
For the 2 last purposes, models can deviate far from biological descriptions but remain very useful: "Kleenex" models !

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Static Graph v.s. Dynamic Behaviour

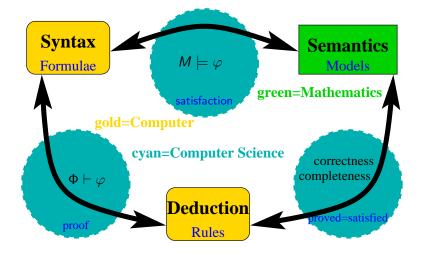
Difficulty to predict the result of combined regulations Difficulty to measure the strength of a given regulation Example of "competitor" circuits

Homeostasy?



Many underlying models \approx 700 qualitative behaviours

Formal Logic: syntax/semantics/deduction



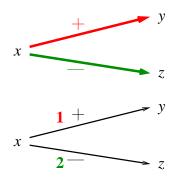
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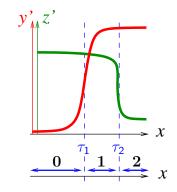


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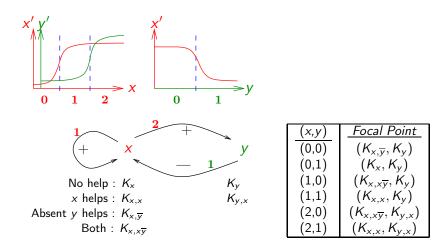
Multivalued Regulatory Graphs





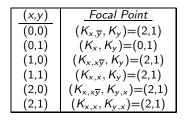
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Regulatory Networks (R. Thomas)

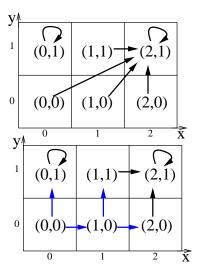


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"desynchronization" by units of Manhattan distance



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CTL = Computation Tree Logic

Atoms = comparaisons : (x=2) (y>0) ...

Logical connectives: $(\varphi_1 \land \varphi_2) \quad (\varphi_1 \implies \varphi_2) \quad \cdots$

Temporal modalities: made of 2 characters

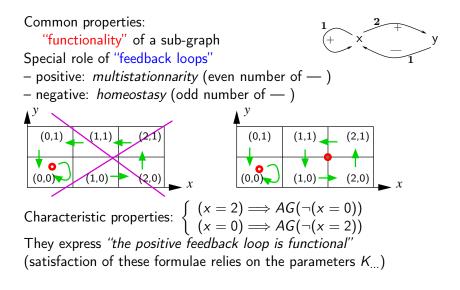
| first character | second character | |
|--------------------------|--------------------------------------|--|
| A = for All path choices | X = ne X t state | |
| | F = for some F uture state | |
| E = there Exist a choice | G = for all future states (Globally) | |
| | $U = \mathbf{U}$ ntil | |

AX(y = 1): the concentration level of y belongs to the interval 1 in all states directly following the considered initial state.

EG(x = 0): there exists at least one path from the considered initial state where x always belongs to its lower interval.

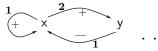
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CTL to encode Biological Properties



The Two Questions

$$\Phi = \{\varphi_1, \varphi_2, \cdots, \varphi_n, H\}$$
 and $\mathcal{M} =$



 $K_{\mathbf{x}} \cdots K_{\mathbf{x},\mathbf{x}} \cdots K_{\mathbf{x},\mathbf{xy}} \cdots$

1. Is it possible that Φ and \mathcal{M} ?

Consistency of knowledge and hypotheses. Means to select models belonging to the schemas that satisfy Φ . (\exists ? $M \in \mathcal{M} \mid M \models \Phi$)

2. If so, is it true in vivo that Φ and \mathcal{M} ?

Compatibility of one of the selected models with the biological object. Require to propose experiments to validate or refute the selected model(s).

\rightarrow Computer aided *proofs* and *validations*

Theoretical Models \leftrightarrow **Experiments**

CTL formulae are satisfied (or refuted) w.r.t. a set of paths from a given initial state

- ► They can be tested against the possible paths of the theoretical models (M ⊨_{Model Checking} φ)
- They can be tested against the biological experiments (Biological_Object ⊨_{Experiment} φ)

CTL is a bridge between theoretical models and biological objects

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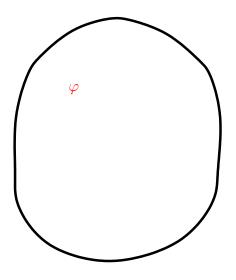
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Generation of biological experiments (1)

Set of all the formulae:

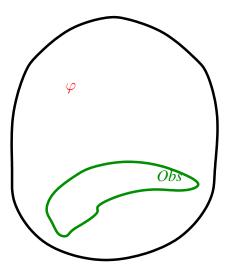
 $\varphi = \mathsf{hypothesis}$



Generation of biological experiments (2)

Set of all the formulae:

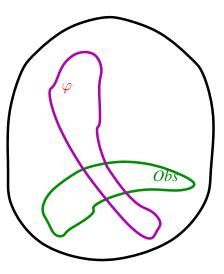
 $\varphi = hypothesis$ Obs = possible experiments



Generation of biological experiments (3)

Set of all the formulae:

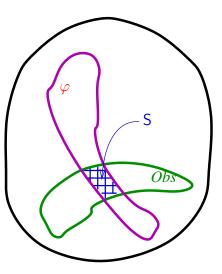
 $\varphi =$ hypothesis Obs = possible experiments $Th(\varphi) = \varphi$ inferences



Generation of biological experiments (4)

Set of all the formulae:

 φ = hypothesis Obs = possible experiments $Th(\varphi) = \varphi$ inferences S = sensible experiments



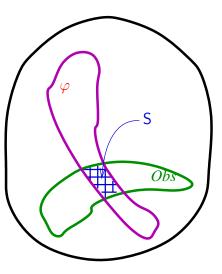
Generation of biological experiments (5)

Set of all the formulae:

 φ = hypothesis Obs = possible experiments $Th(\varphi) = \varphi$ inferences S = sensible experiments

Refutability:

$$S \Longrightarrow \varphi$$
 ?



Generation of biological experiments

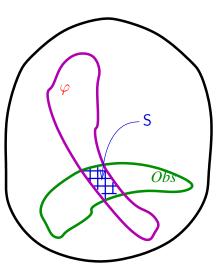
Set of all the formulae:

 φ = hypothesis Obs = possible experiments $Th(\varphi) = \varphi$ inferences S = sensible experiments

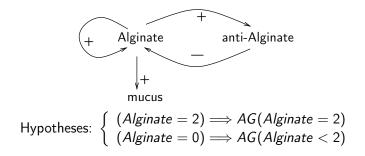
Refutability:

 $\mathsf{S} \Longrightarrow \varphi$?

Best refutations: Choice of experiments in S ? \dots optimisations



How to validate a multistationnarity



Assume that only *mucus* can be observed: Lemma: $AG(Alginate = 2) \iff AFAG(mucus = 1)$ (... formal proof by computer ...)

 \rightarrow To validate: (*Alginate* = 2) \implies *AXAG*(*mucus* = 1)

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$(Alginate = 2) \implies AXAG(mucus = 1)$

Karl Popper:

| $A \Longrightarrow B$ | true | false |
|-----------------------|------|-------|
| true | true | false |
| false | true | true |

to validate = to try to refute *thus A=false is useless* experiments must begin with a pulse

The pulse forces the bacteria to reach the initial state Alginate = 2. If the state is not directly controlable we need to prove lemmas:

(something reachable) \implies (Alginate = 2)

General form of a test:

(something <u>reachable</u>) \implies (something <u>observable</u>)



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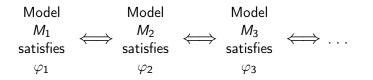
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Hypothesis driven model simplifications

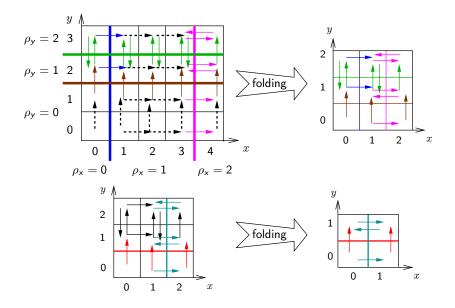
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Successive simplified views of the studied biological object:



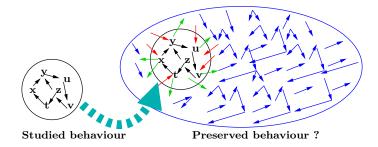
Simplifications via level folding



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Simplifications via subgraphs

Embeddings of Regulatory Networks:



Necessary and sufficient condition on the *local* dynamics of the "input frontier"

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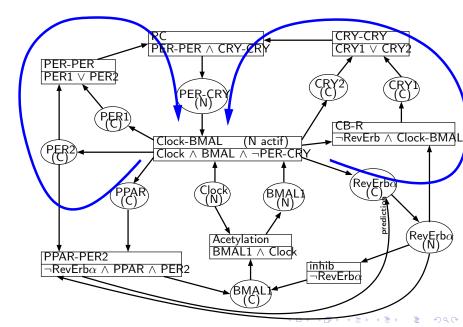
... Also fusion of genes, etc.



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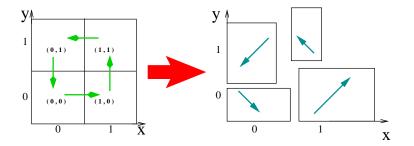
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"Data Base" interaction graph



The target question

Impact of the day length on the persistence of the circadian circle ? \implies framework with time delays:



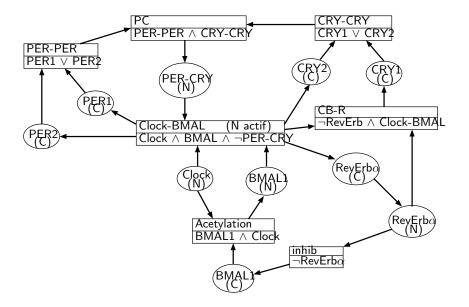
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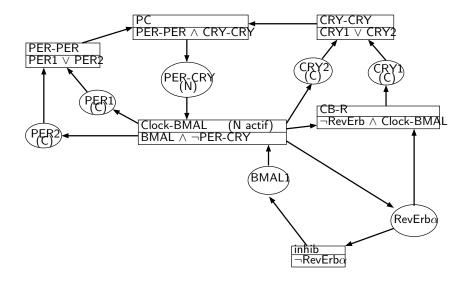
(size of rectangular areas = delays)

+ extension of temporal logic with delays...

Fold levels and remove PPAR

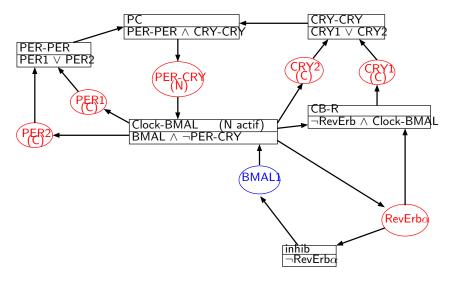


Remove Clock and "tunnel" pathways



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Separate inhibitors/activators of Clock-BMAL



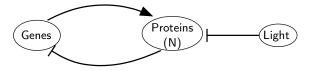
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Fusion of all inhibitors

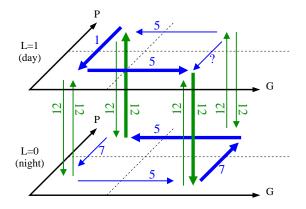
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and Light prevents PER-CRY to enter the nucleus:



12 hours model

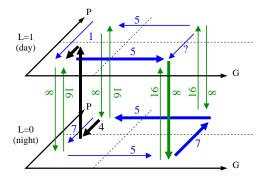


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Winter model

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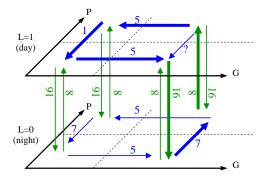
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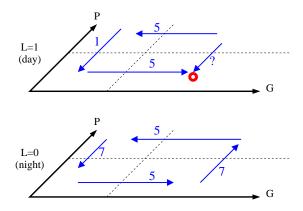
Summer model

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Jet lag + training



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Yet far from automatic simplifications but...

Abstract interpretation at



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Model reduction at



Acknowledgements

- Observability Group, Epigenomics Project (Genopole[®])
- Janine Guespin (Rouen)
- Franck Delaunay (Nice)
- Jean-Paul Comet (Nice)
- Camille Massot (Polytech, BIMB)
- Amélie Cessieux (Polytech, BIMB)

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Option BIMB en Génie Biologique

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Take Home Messages

Make explicit the hypotheses that motivate your research

A far as possible formalize them to get a computer aided approach Behavioural *properties* are as much important as *models* Mathematical models are not reality: let's use this freedom ! (several views of a same biological object)

Modelling is significant only with respect to the considered experimental *reachability* and *observability* (for refutability)

Formal proofs can suggest wet experiments

"Kleenex" models help understanding main behaviours