Aligning component upgrades

Roberto Di Cosmo
Univ Paris Diderot, Sorbonne Paris Cité,
Laboratoire PPS, UMR 7126,
F-75205 Paris France
roberto@dicosmo.org

Olivier Lhomme
IBM France,
1681, route des Dolines,
06560 Sophia Antipolis, France
om.lhomme@gmail.com, olivier.lhomme@fr.ibm.com

Claude Michel
I3S (UNS-CNRS),
2000 route des Lucioles, BP 121,
06903 Sophia Antipolis Cedex, France
Claude.Michel@i3s.unice.fr

Modern software systems, like GNU/Linux distributions or Eclipse-based development environment, are often deployed by selecting components out of large component repositories. Maintaining such software systems by performing component upgrades is a complex task, and the users need to have an expressive preferences language at their disposal to specify the kind of upgrades they are interested in. Recent research has shown that it is possible to develop solvers that handle preferences expressed as a combination of a few basic criteria used in the MISC competition, ranging from the number of new components to the freshness of the final configuration. In this work we introduce a set of new criteria that allow the users to specify their preferences for solutions with components aligned to the same upstream sources, provide an efficient encoding and report on the experimental results that prove that optimising these alignment criteria is a tractable problem in practice.

1 Introduction

Recent research, in part fostered by the Mancoosi project, has focused on the complex problem of handling upgrades in component based software systems, with a particular attention to the case of GNU/Linux distributions, which contain several tens of thousands of components. Installing components (called packages in the world of distributions) may be complex: each component may need some extra components to be installed, as described in its metadata by dependencies, and may be incompatible with some other ones, as described in its metadata by conflicts. Indeed, determining whether a component can be installed is NP-complete, but problem instances arising in practice turn out to be tractable by modern solvers. These practical results opened the way to explore not just the question of finding a way of installing some components, but the best way of doing so, according to some criteria that capture the user preferences and needs.

The Mancoosi International Solver Competition (MISC) was established with the goal to distill interesting problems from real-world GNU/Linux distribution upgrade scenarios, and present them to the solver research community. The problems are encoded in documents written using common format, CUDF, that describe the universe of available components with their interdependencies and the user preferences.
Table 1: Optimization criteria

<table>
<thead>
<tr>
<th>Criteria</th>
<th>Expression</th>
</tr>
</thead>
<tbody>
<tr>
<td>removed ( (I,S) )</td>
<td>( { \text{name}</td>
</tr>
<tr>
<td>new ( (I,S) )</td>
<td>( { \text{name}</td>
</tr>
<tr>
<td>changed ( (I,S) )</td>
<td>( { \text{name}</td>
</tr>
<tr>
<td>notuptodate ( (I,S) )</td>
<td>( { \text{name}</td>
</tr>
<tr>
<td>unsatrec ( (I,S) )</td>
<td>( { (\text{name}, \text{v}, \text{c}) - \text{v} \text{ is an element of } V_p(S, \text{name}) )  and ( (\text{name}, \text{v}) \text{ recommends } ..., \text{c}, ... \text{ and } \text{c} \text{ is not satisfied by } S } )</td>
</tr>
</tbody>
</table>

request; the solvers are requested to find solutions that are ranked according to user preferences which are currently built by composing a few basic criteria using aggregation functions like the lexicographic ordering.

There are five basic criteria currently used in MISC: removed, changed, new, notuptodate and unsatrec, which capture intuitive properties of a solution to an upgrade problems, like the number of removed components or the number of components that are not the most up to date. They are summarised in Table 1 where \( I \) is the initial installation and \( S \) is a proposed new installation. We write \( V_p(X, \text{name}) \) for the set of versions in which \( \text{name} \) (the name of a component) is installed in \( X \), where \( X \) may be \( I \) or \( S \). That set may be empty (\( \text{name} \) is not installed), contain one element (\( \text{name} \) is installed in exactly that version), or even contain multiple elements in case a component is installed in multiple versions.

These criteria and aggregation functions are an important starting point for this research, but are not sufficient to capture all the important properties of an upgrade: identifying new basic criteria and new aggregation function is an important activity, that will help improve the algorithms and tools available for maintaining the complex software systems of tomorrow.

Synchronization is a general common sense behavior; in the context of complex software systems, we can expect a better robustness from synchronized components for multiple reasons. Metadata, through dependencies, can express some kind of synchronizations, but only the strong and known ones. The general problem of synchronization is not addressed by metadata. For example, binaries and sources are not required to be of the same version, although a developer could expect such a synchronization.

**Contribution** In this paper, we present a new criterion, component alignment, which measures the synchronization of closely related components in an installation and which is not expressible using the existing criteria used in the MISC competition. Then, we show how to encode it using current solver technology, and present experimental results that show that it is tractable in practice.

## 2 Component alignment

In complex software systems, like GNU/Linux distributions, components do not exist in isolation, but are very often related to each other, even if they may be installed independently: the documentation of a program, for example, is not necessary to run it, but they are both present, the user expects them to be of the same version, or, in other terms, to be aligned.
With the current basic preferences used in MISC, it is not possible to express this alignment property, and one can see that even the best solutions in the MISC 2010 competition may contain surprising component combinations: looking for example at the solutions found by the competition entrants for the problem `eeee44ce` in the trendy track, one can find surprising combinations like

<table>
<thead>
<tr>
<th>Package</th>
<th>Version</th>
</tr>
</thead>
<tbody>
<tr>
<td>aptitude-doc-fr</td>
<td>0.6.1.5-3</td>
</tr>
<tr>
<td>aptitude</td>
<td>0.4.11.11-1+b2</td>
</tr>
</tbody>
</table>

or even

<table>
<thead>
<tr>
<th>Package</th>
<th>Version</th>
</tr>
</thead>
<tbody>
<tr>
<td>linux-libc-dev</td>
<td>2.6.32-9</td>
</tr>
<tr>
<td>linux-source-2.6.30</td>
<td>2.6.30-8squeeze1</td>
</tr>
</tbody>
</table>

These are potential sources of confusion for a user that finds documentation way ahead of the installed binaries or sources way behind the installed libraries. In the case of mixed versions of important libraries, like `gs` in version `8.64 dfsg-1+squeeze1` which is used with `gs-common` version `8.71 dfsg-4` in the same example, one can even experience real incompatibilities, due to combination of components that have not been thoroughly tested together.

Obtaining an aligned installation by hand is quite painful, because of the number of involved packages: it is really necessary to be able to express the preference concisely via a criterion.

To help the users that want to avoid these inconsistencies, we propose to exploit the information about the package `source`, which is present in the metadata of mainstream distributions.

In Debian, for example, packages which are built from the same source package carry in their metadata two pieces of information:

- a `source` property, that specifies the name of the source package; for example, both packages related to the Linux kernel in the example above have a `source` property with the same value `linux-2.6`.
- the version of the source used to build them; this information is encoded in the CUDF documents coming from Debian distributions in a `sourceversion` property; for example, the two packages related to the Linux kernel in the example above are built from two different versions, `2.6.32-9` and `2.6.30-8squeeze1`, of the same source `linux-2.6`.

Using this information, one can define what it means for an installation to be aligned.

**Definition 1 (Alignment)** An installation $I$ is source aligned if all installed packages built from a same source $s$ are actually built from the same version of this source.

In other terms, $I$ is aligned if all packages $p_i$ having the same value for the `source` property also have the same value of the `sourceversion` property.

We remark here that the version of a package, and the version of the source from which they are built do not necessarily coincide, and packages built from the same version of the same source may carry different package versions, so that using the version of the source as an alignment criterion is the best way of knowing whether a set of packages is aligned, without the need to guess similarity of packages by inspecting their package versions.

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3See [http://data.mancoosi.org/misc2010/results/problems/debian-dudf/eeee44ce-5407-11df-b11f-00163e7a6f5e. cufd.bz2](http://data.mancoosi.org/misc2010/results/problems/debian-dudf/eeee44ce-5407-11df-b11f-00163e7a6f5e. cufd.bz2)
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Notations In the following, we write $\mathcal{S}$ for the set of sources of the problem to solve.
We note $\{p_i\}_{i=1..n}$ the set of all available packages. For simplifying the notation, $p_i$ will also denote a 0-1 variable that expresses that package $p_i$ is installed; when the context is not enough to resolve the ambiguity we write package $p_i$ or variable $p_i$.

The relationships between the sources, the packages and their versions will be expressed with the following functions:

- $V(s)$ denotes the set of versions of source $s \in \mathcal{S}$;
- $V(p)$ denotes the version of the source of package $p$;
- $P(s,v)$ denotes the set of packages belonging to version $v$ of source $s$;
- $S(p)$ denotes the value of the source property of package $p$.

For example, $p \in P(s,v) \iff V(p) = v$ and $S(p) = s$.

3 Measuring unalignment

In order to choose among different possible installations, we need to be able to measure how far we are from an aligned solution; for this, we need a measure of unalignment of a solution to a user query, that can be then used as an objective function to minimize.

It turns out that there are quite a few different ways of defining such a notion, with varying cost and expressiveness. We discuss them in the following sections, where we present the different possible definitions. An encoding for MIP solvers, along the lines of [8], is given in detail in Section 4.

3.1 Counting unaligned packages

A first approach to building a measure of unalignment is to count the number of packages $p_i$ which are installed and not source aligned. This can be expressed formally as the cardinality of a set:

$$unaligned_p = \text{card}\{p_i | i \in [1..n], p_i = 1, \exists j p_j = 1, S(p_j) = S(p_i), V(p_j) \neq V(p_i)\}$$

Note that in our notation, variables $p_i$ and $p_j$ are equal to 1 mean that packages $p_i$ and $p_j$ are installed. The above set contains all packages that are installed and such that another package with the same source in another version is also installed.

To obtain an installation that is as aligned as possible, it is then enough to minimize $unaligned_p$, the cardinality of the set.

3.2 Counting (sorted) unaligned package pairs

A second approach is to count the number of pairs of packages $(p_i, p_j)$ which are both installed and not aligned. This can be done by computing the cardinality of a slightly different set:

$$unaligned_{pp} = \text{card}\{(p_i, p_j) | i, j \in [1..n], i < j, p_i = 1, p_j = 1, S(p_j) = S(p_i), V(p_j) \neq V(p_i)\}$$

The interest of this approach is to be much more discriminating than the $unaligned_p$ criteria (see Section 3.5). Nevertheless, a drawback may be that, as it implicitly weights a cluster up to the square of its size, a small qualitative improvement of a large and very unaligned cluster may strongly dominate clear qualitative improvements of some other smaller or almost aligned clusters.
3.3 Counting version changes

In this third approach, the size of the cluster is not as important as in the unaligned<sub>pp</sub> criteria: it counts the number of version changes in a cluster. For example, consider a cluster with six installed packages that involve three different source versions: there will be two version changes. Formally:

\[
\text{unaligned}_{vc} = \sum_{s \in \mathcal{S}} \max(0, \text{numberOfVersions}(s) - 1)
\]

where:

\[
\text{numberOfVersions}(s) = \text{card}\{V(p_i) | i \in [1..n], p_i = 1, S(p_i) = s\}
\]

Note that numberOfVersions(s) is the number of installed versions of the source s; thus, when this number is greater than 0, we need to subtract 1 to get the number of version changes.

3.4 Counting unaligned source clusters

Finally, one can use a much coarser granularity, counting only the source clusters which are unaligned, independently of the number of pointwise unalignments among packages of the same cluster, by using

\[
\text{unaligned}_{c} = \text{card}\{s | s \in \mathcal{S}, \exists i \in [1..n], \exists j \in [1..n], p_i = 1, p_j = 1, S(p_i) = S(p_j) = s, V(p_j) \neq V(p_i)\}
\]

3.5 Discussion of the different alignment criteria

The different alignment criteria differ by their weighting policies. The number of unaligned source clusters unaligned<sub>c</sub> and the number of unaligned packages unaligned<sub>p</sub> are very close, except that the criterion unaligned<sub>c</sub> does not take into account the size of the clusters, whereas the criterion unaligned<sub>p</sub> weights a cluster by its size (each time a cluster of size k is unaligned, k packages are unaligned). The criterion unaligned<sub>pp</sub> is more discriminating by weighting a cluster by its pairwise unalignment, which may be really interesting, but it makes the implicit assumption that packages of a cluster are totally interdependant. When this assumption is too strong and the size of the cluster is large, the weight of a k-sized cluster can be as large as k<sup>2</sup>, and alignments in large clusters may dominates too strongly alignments in small clusters. The criterion unaligned<sub>vc</sub>, based on version changes, provides an interesting intermediate solution: the weight of the cluster is the number of different versions in that cluster.

To see in practice what each of the above criterion actually captures, it is useful to compare the results on a simple example. Let’s consider a cluster \(c = \{p_1, p_2, p_3, p_4\}\) comprising 4 packages of the same source, with package versions among 1, 2, 3, 4, and a few possible unaligned configurations.

<table>
<thead>
<tr>
<th>version configuration</th>
<th>unaligned packages</th>
<th>unaligned pairs</th>
<th>unaligned version changes</th>
<th>unaligned clusters</th>
</tr>
</thead>
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<tr>
<td>1,1,1,1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>1,1,2,1</td>
<td>4</td>
<td>3</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>1,1,2,2</td>
<td>4</td>
<td>4</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>1,1,2,3</td>
<td>4</td>
<td>5</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>1,2,3,4</td>
<td>4</td>
<td>6</td>
<td>3</td>
<td>1</td>
</tr>
</tbody>
</table>
4 Efficiently encoding the criteria using MIP

This section describes an integer programming encoding of the unaligned criteria presented above. It is particularly efficient in practice with a MIP solver. Note that a clausal form of these criteria can also be obtained for using a SAT solver (see the Appendix).

As a first step, the problem is reduced to the subset of sources with more than one source version.

4.1 packages

The number of unaligned packages is computed using the following formulae

\[
nu_{\text{packages}} = \sum_{p_j \in P(s,v), v \in V(s)} nu_{p_j}
\]

where \(nu_{p_j}\) is a binary variable whose value is one if \(p_j\) is installed and not aligned and zero otherwise.

Each \(nu_{p_j}\) is handled by the following set of constraints

\[
nu_{p_j} \leq p_j
\]

which forces \(nu_{p_j}\) to 0 if package \(p_j\) is not installed, and

\[
nu_{p_j} \leq \sum_{v \in V(S(p_j)), v \neq V(p_j)} i_{s,v}
\]

where \(s = S(p_j)\) and \(i_{s,v}\) is binary variable whose value is 1 if any package of version \(v\) from source \(s\) is installed and zero otherwise. Therefore, the previous constraint forces \(nu_{p_j}\) to zero if none of the other versions of source \(s\), different from \(V(p_j)\), has an installed package. \(nu_{p_j}\) is also involved in the following set of constraints

\[
\forall v \in V(S(p_j)), v \neq V(p_j), nu_{p_j} + 1 \geq p_j + i_{s,v}
\]

which ensures that if \(p_j\) is installed and one of the versions of \(s\) different from the source version of \(p_j\) has an installed package, then \(nu_{p_j}\) is set to one.

Finally, constraints are added to handle the \(i_{s,v}\) variables. The first constraint ensures that \(i_{s,v}\) gets the value zero if none of the packages of version \(v\) from source \(s\) is installed

\[
i_{s,v} \leq \sum_{p_j \in P(s,v)} p_j
\]

The second set of constraints sets \(i_{s,v}\) to 1 whenever at least one of the packages of version \(v\) from source \(s\) is installed

\[
\forall p_j \in P(s,v), p_j \leq i_{s,v}
\]

Note that variables \(i_{s,v}\) are also used in the encoding of the two last unaligned criteria.
4.2 pairs

The number of unaligned pairs

\[ nu_{pairs} = \sum_{p_j \in P(s,v), v \in V(s), s \in S, p_k \in P(s,v'), v' \in V(s), v' \neq v} u_{p_j,p_k} \]

where each \( u_{p_j,p_k} \) is subject to the three following constraints:

\[ u_{p_j,p_k} \leq p_j \land u_{p_j,p_k} \leq p_k \land u_{p_j,p_k} + 1 \geq p_j + p_k \]

The two first constraints insure that \( u_{p_j,p_k} = 0 \) if either \( p_j \) or \( p_k \) is not installed. Last constraint sets \( u_{p_j,p_k} \) iff both \( p_j \) and \( p_k \) are installed.

4.3 version changes

The number \( nu_{vc} \) of version changes is given by the following formulae:

\[ nu_{vc} = \sum_{s \in S} nc_s \]

where each \( nc_s \) is subject to

\[ nc_s = nb_{inst,s} - \delta_s \]

where each \( \delta_s \) is subject to

\[ |V(s)| + \delta_s \geq nb_{inst,s} \land nb_{inst,s} \geq \delta_s \]

The first constraint sets \( \delta_s \) to 1 iff \( nb_{inst,s} \geq 1 \), and the second one sets \( \delta_s \) to 0 iff \( nb_{inst,s} = 0 \). The \( nb_{inst,s} \) variable simply sum up the number of installed source versions (i.e., the number of source versions with at least one installed package). Thus,

\[ nb_{inst,s} = \sum_{v \in V(s)} i_{s,v} \]

4.4 clusters

The number of unaligned clusters of source is given by the following formulae:

\[ nu_{clusters} = \sum_{s \in S} u_s \]

where each \( u_s \) is subject to

\[ |V(s)| * u_s + 1 \geq nb_{inst,s} \land nb_{inst,s} \geq 2 * u_s \]

The first constraint sets \( u_s \) to 1 iff \( nb_{inst,s} \geq 2 \), while the second one forces \( u_s \) to 0 iff \( nb_{inst,s} \leq 1 \). \( nb_{inst,s} \) has the same definition as in the unaligned version changes.
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<table>
<thead>
<tr>
<th>MISC problem id</th>
<th>size (#srcs,#vs,#pkgs,#pairs)</th>
<th>removed</th>
<th>packages</th>
<th>pairs</th>
<th>version changes</th>
<th>clusters</th>
</tr>
</thead>
<tbody>
<tr>
<td>103c9978</td>
<td>183,531,531,377</td>
<td>0.71</td>
<td>1.10</td>
<td>1.04</td>
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</tr>
<tr>
<td>1dce258</td>
<td>3833,12319,12319,15595</td>
<td>5.00</td>
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<td>1.06</td>
<td>1.18</td>
<td>1.09</td>
</tr>
</tbody>
</table>

Total time 64.92 137.10 129.97 171.84 132.41

Figure 1: Running time (s) and number of unalignments on the MISC-2010 Debian problem instances

5 Experimental validation

We implemented the four alignment criteria introduced above in an experimental branch of the mccs tool, which uses MIP instead of the Boolean encodings, and includes several optimizations with respect to the simple encodings detailed above.

We have run the solver on the Debian category of the problems of the MISC-2010 competition and of the 4th run of the Misc Live competition with a realistic optimization function that requires, in lexicographic order to first minimize removal, and then minimize unalignment, using each of the four different criteria for unalignment. The results of running this experiments on an Intel Core I7-2720QM at 2.20GHz are given in Figure 1 for the MISC-2010 competition and in Figure 2 for the 4th run of the Misc Live competition. In these tables, the size column gives respectively, the number of sources (with more than one version) of the problem, the total amount of versions, the total amount of packages (corresponding to the selected sources/versions), and, the number of unique pairs. The removed column gives the time (in seconds) required to optimise the problem according to the sole removed criterion, as well as, in brackets, the number of unaligned packages, pairs, version changes and clusters of the solution. Last four columns give the amount of time required to solve the problem minimizing removal and the chosen unalignment, as well as, in brackets, the number of unalignments. Note that, for the sake of fairness, CPLEX, the underlying MIP solver, has been limited to one thread.

These two sets of results show a strong relationship between the structure of the problem, the chosen unalignment measure and the time required to solve the problem. However, these results seems to indicate that the version change alignment criterion offers a good trade off between discriminating power and running time.

http://users.polytech.unice.fr/~cpjm/misc/mccs.html

Though the two sets of Debian problems share some problem IDs, there are different problems as testified by the problem sizes and the different times.
### Discussion

Aligning components in a software installation is an important issue; we have shown that it is possible to capture this property in several ways, according to the discriminating power one looks for, and that a state of the art MIP solver such as CPLEX has a running time on realistic use cases that is acceptable.

An important question is whether a similar performance can be attained using different solving approaches, like PBO, MaxSat or Answer Set Programming, which are present in the MISC competition. We propose that the different measures of unalignment introduced here be incorporated in future MISC competitions, and that component installers offer them to the users.

For future work, it would be interesting to allow the users to fine-tune the subset of source packages on which the alignment is required, by introducing a more general criterion \texttt{unaligned(clusters:v1,...,vn)}, that evaluates unalignment only on the clusters for \texttt{v1}, ..., \texttt{vn}: this does not present significant technical difficulties and can be done by generating the constraints only for the specified source clusters.

Alignment being only a restricted definition of a more general synchronization criterion, it may be equally important to synchronize some packages that are not built from the same sources, but are closely related. Such synchronization relations between packages could be expressed by extending metadata.

### References

A Encoding unalignment for SAT

It is possible to write natural encodings of the different criteria for SAT; we present here the ones for the packages and package pairs criteria.

packages The definition can be encoded as

\[ \text{unaligned}_p \iff p \land \left( \bigvee_{S(q_i)=S(p)\land V(q_i)\neq V(qp)} q_i \right) \]

For minimizing unalignment, it is enough to use the clauses coming from the dominance relation

\[ \text{unaligned}_p \iff p \land \left( \bigvee_{S(q_i)=S(p)\land V(q_i)\neq V(qp)} q_i \right) = \text{unaligned}_p \iff \left( \bigvee_{S(q_i)=S(p)\land V(q_i)\neq V(qp)} p \land q_i \right) \]
= \bigwedge_{S(q_i) = S(p) \land V(q_i) \neq V(qp)} (\text{unaligned}_p \iff p \land q_i)

= \bigwedge_{S(q_i) = S(p) \land V(q_i) \neq V(qp)} \neg\text{unaligned}_p \lor \neg p \lor \neg q_i \quad (3)

\textbf{pairs} \quad \text{For each package pair } (p_i, p_j) \text{ which is not aligned, build a literal } \text{unaligned}_{p_i, p_j} \text{, which is true iff both } p_i \text{ and } p_j \text{ are installed.}

\text{unaligned}_{p_i, p_j} \iff p_i \land p_j

\text{For minimizing unalignment, it is enough to use the clauses coming from the dominance relation}

\text{unaligned}_{p_i, p_j} \iff p_i \land p_j =

= \neg p_i \lor \neg p_j \lor \text{unaligned}_{p_i, p_j} \quad (3)